

**RECEIVER DEPENDENT SELECTION OF A WORST-CASE TIMING  
EVENT FOR STATIC TIMING ANALYSIS**

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## RECEIVER DEPENDENT SELECTION OF A WORST-CASE TIMING EVENT FOR STATIC TIMING ANALYSIS

### FIELD OF THE INVENTION

[0001] The field of the present invention relates to electronic design automation, and  
5 more particularly, to methods and systems for timing analysis of electronic circuit blocks.

### BACKGROUND OF THE INVENTION

[0002] Advances in silicon technology increasingly allow larger and more complex  
10 designs of electronic circuits to be formed on a single chip. For example, modern electronic  
designs have millions or tens of millions of transistors. At the same time, market demands push  
circuit designers to create these designs rapidly and efficiently. A recent trend to increase the  
speed and efficiency of the design process involves the re-use, or recycling, of electronic circuit  
blocks or subsystems, commonly referred to as cores, Intellectual Properties (IPs), or virtual  
15 component blocks (VCs). Once the design for a virtual component block has been tested and  
verified, it can be re-used in other applications that may be completely distinct from the  
application which led to its original creation.

[0003] For example, a subsystem for a cellular phone application specific integrated  
circuit (ASIC) may contain a micro-controller, a digital signal processor, and other electronic  
20 components. After the design for the cellular phone subsystem has been tested and verified, it  
could be re-used as a virtual component block in a circuit design for an automotive application.  
The reuse of virtual component blocks allows a designer to complete the design process much  
faster than building the entire design from scratch, and avoids the need for debugging, testing  
and verification of the subsystems embodied in the virtual component block.

25 [0004] While virtual components have been found to be convenient for expediting and  
simplifying the circuit design process, the successful use of virtual component blocks hinges on  
the ability of the designer to accurately characterize their timing and functionality. A number of  
techniques have been proposed and developed for performing timing analyses on virtual  
component blocks, among which static timing analysis (STA) is most widely used.

[0005] Static Timing Analysis is used in the process of verifying the timing correctness of a digital circuit design during one clock cycle, without the need for simulating the circuit.

During the STA process, a worst-case structural (or topological) delay between a circuit's inputs and outputs is calculated. For example, a model of a signal that propagates through

5 combinational logic includes an analysis of the longest and the shortest paths spanning between a launching register and a capturing register in order to determine, in the worst case, whether the signal arrives at the capturing register during the active pulse of the clock cycle.

[0006] In STA, a rising or falling voltage transition is abstracted by a timing event (TE), to approximate the transition of the actual waveform using two of its parameters, the

10 arrival time and slew rate. The arrival time of the transition is based on the time that the voltage of the waveform reached a user-selected reference voltage ( $V_{ref}$ ), or trip point, such as  $0.5V_{dd}$  for example. The slew rate is determined by an amount of time for the waveform to move from one given voltage level,  $V_{th1}$ , to a second given voltage,  $V_{th2}$ . For example, the slew rate may be based on the amount of time that the waveform takes to transition from a voltage of  $0.2V_{dd}$  to

15  $0.8V_{dd}$ . However, given the complexity of modern designs, the approximation of the waveform provided by the TE may be insufficient to verify the design's timing correctness.

[0007] For example, in a STA process, a design is represented by an acyclic directed graph, called a Timing Graph (TG), where timing nodes represent intermediate in the design and edges represent delays along nets and library cells. The TG is built using an assumption that the

20 delay through a given stage is dependent only on the waveform that is received by the stage, and on the interconnects of the stage. During the analysis, TEs are propagated forward in the TG from input nodes to output nodes. If a stage has multiple inputs, the corresponding node in the TG receives multiple TEs. A worst-case TE is selected from the multiple TEs at the timing node for further propagation to downstream logic elements during the analysis.

25 [0008] In this conventional approach, only the arrival time of the timing event at the given node is used as the criterion for selecting the worst-case timing event, and the slew rate is typically not considered. However, ignoring the slew rate can lead to optimistic results for the critical path delay that is verified during this process, especially if a skewed gate (a gate with a trip point away from  $0.5V_{dd}$ ) is used. For example, a TE may be selected as the worst-case

30 according to the conventional approach, which is based on the arrival time of the TE on the

particular node. However, this “worst-case” TE may not be the worst-case TE if the TEs are propagated to the output of a skewed receiver, because the slew differences of the signals may have a strong impact on the delay over the receiving stage.

[0009] To prevent optimistic results, conventional tools [CTEref] allow a user to  
5 construct a new timing event by combining the worst arrival time, (such as the maximum time for a max delay analysis or the minimum time for min delay analysis) and the worst slew rate (such as the lowest or highest slew rate for, respectively, max or min delay analysis). The arrival time and slew rate of the new “worst-case” timing event is therefore a combination of various parts of different timing events, rather than a selection of one of the TEs that arrives at the  
10 receiving gate. While this approach is usually conservative, it may lead to optimistic results if the receiving gate is skewed. For example, if an inverter is skewed towards a low voltage (e.g. with similar sizes of p- and n- devices), a rising transition with a lower slew rate can result in a lower delay over the inverter.

[0010] Furthermore, the conventional analysis does not consider properties of the  
15 receiving gate itself when determining the worst-case transition. This causes results based on conventional criteria to be either optimistic or very conservative, and may lead to functional failures or over design.

[0011] Therefore, more accurate timing verification methods are needed. [ICCAD ref].

## SUMMARY OF THE INVENTION

[0012] A method for determining a worst-case timing event is disclosed. The method includes determining a plurality of output arrival times and slew rates for the plurality of input timing events based on the timing model and load of receiving gate, and selecting a worst-case  
5 input timing event from the plurality of input timing events based on the arrival times computed on the output of the receiving gate.

**BRIEF DESCRIPTION OF THE DRAWINGS**

[0013] **Figure 1** shows an example of a circuit design partitioned into stages and into a timing graph to perform receiver-dependent static timing analysis.

5 [0014] **Figure 2** shows a schematic example of a worst-case transition selection using receiver-dependent static timing analysis.

[0015] **Figure 3** shows an example of a circuit for which conventional selection criterion leads to optimistic results, and receiver dependent analysis leads to more accurate results.

10 [0016] **Figure 4** shows simulation results of transitions applied to the circuit in **Figure 3**, including a worst-case transition selected by the receiver dependent method.

[0017] **Figure 5** shows an example of a stage of a complex gate with pull-down stacks having unbalanced strengths, causing different output slew rates which are analyzed by the receiver dependent worst-case selection method.

15 [0018] **Figure 6** shows examples of simulation results of transitions applied to the stage shown in **Figure 5**.

[0019] **Figure 7** shows results of circuit simulations of the circuit shown in **Figure 3** having an upsized driver to improve the input slew of the circuit, which is considered during the receiver dependent selection method.

20 [0020] **Figure 8** shows example of a circuit for which logic relations between neighboring nets can lead to different slews and arrival times on the input of receiver if effects of noise-on-delay are considered in the receiver dependent STA.

**DETAILED DESCRIPTION**

[0021] A method of static timing analysis selects a worst-case timing event, or transition, based on characteristics of the receiving gate, during the design and verification process of an electronic circuit, so that the circuit can be fabricated onto a VLSI chip. Because the receiver-dependent process selects the worst-case timing event at the input of the receiving gate based on the receiving gate's characteristics, such as the gate's delay for example, the receiver-dependent STA results are more accurate than methods that only consider the input timing event's features.

[0022] The receiver-dependent STA selects the worst-case timing event from multiple timing events that are sent by one or more driving gates. The selected worst-case timing event is then propagated through the receiving gate to the downstream logic to determine the delays of the circuit design. Calculated delays include the largest and smallest delays along various sensitizable paths that connect sampling blocks (such as flip-flops or latches), or primary inputs and outputs of the circuit, in the direction of the data flow, for example.

[0023] Figure 1 shows an example of a circuit design 100 that is partitioned into stages x, y, z, and p to generate the TG 110. The nodes x, y, z, and p of the TG correspond to inputs of the gates where timing events are determined. The timing arcs 102, 103, 104 of the circuit represent sensitizations, or delays, encountered by signals as they propagate through the gates 105 and 106. These sensitizations are represented by the timing events 112, 113, 114 of the TG 110.

[0024] During the analysis, the TG 110 is traversed in topological order from the input nodes (sources) x and y to the output node (sink) p corresponding, respectively, to primary inputs and outputs of the circuit 100. The multiple sensitizations (timing arcs) 102, 103 over the NAND gate 105 of circuit 100 leads to multiple timing events 112, 113 that are received by node z of TG 110. The timing event with the worst-case transition is selected to be propagated through the input of inverter 106 at node z and is output by the inverter at node p. This worst-case selection process is based on characteristics of the inverter.

[0025] Figure 2 shows that the two transitions, 112 and 113, arriving at node z, have different arrival times and slews: the transition with the later arrival time, 112, has a smaller slew

than the earlier transition 113. These different slews and arrival times of the transitions arriving at the input of the inverter are used, along with the receiving inverter's characteristics, in selecting the worst-case timing event 113, which is schematically shown in **Figure 2**. For example, the selection method can consider the effects of the inverter on the transitions from the arrival times and slews of the transitions 112' and 113' at the receiver's output to identify the worst-case input transition, 113. The receiver dependent selection process is therefore more accurate than a conventional selection method, which chooses the event with the later arrival time at the gate's input,  $\max \{T_{i,n}\}$ .

[0026] For example, considering the input transitions as shown in **Figure 2**, input transition 112, which has the later arrival time, is chosen as the worst-case transition for further propagation by a conventional method. But when both signals are propagated to the output of the inverter, the transition 112 is not the worst-case, because the inverter's characteristics affect the output times of the transitions 112' and 113'. As shown in **Figure 2**, the output delay for the signal 113 that travels along x to p is longer than the output delay of the signal 112 that travels along path y to p. Therefore, the signal 112 is selected as having the worst-case transition using the receiver dependent selection method.

[0027] The output time,  $T_o$ , of a transition on the output node OUT may be computed based on the transition's arrival time at the input of the inverter,  $T_i$ , and the delay over the gate to the output,  $D_g$ :

$$T_o = T_i + D_g \quad (1)$$

where the times  $T_o$  and  $T_i$  of the output and input transitions are selected by a user to be the time each reaches its crossing time  $V_{ref}$ .

[0028] The delay  $D_g$  of a gate depends in part upon the slew of the input transition, and the capacitive load at the gate's output. The gate delay,  $D_g$ , can therefore be represented as an algebraic function of the input slew,  $S_i$ , and the gate's total capacitive load,  $C$  [k-factor\_ref]:

$$D_g = F(S_i, C) \quad (2)$$

[0029] Similarly, the output slew can be represented as a function of input slew and capacitive load:

$$S_o = Q(S_i, C) \quad (3)$$



[0030] For  $N$  timing events propagated to an input of a receiving gate,  $T_{i,n}$ ,  $S_{i,n}$  denote, respectively, arrival times and slews of an  $n$ -th timing event at the input of the receiver, for  $n=1..N$ , where  $N$  is number of the timing events. The corresponding output transition is then denoted as  $\{T_{o,n}, S_{o,n}\}$ . These values are calculated by introducing input slews,  $S_{i,n}$ , and the total load capacitance  $C$  of the net driven by the receiver, into the gate delay model described by equations (2) and (3), such that:

$$D_{g,n} = F(S_{i,n}, C) \quad (4)$$

$$S_{o,n} = Q(S_{i,n}, C) \quad (5)$$

[0031] The values of  $D_{g,n}$  and  $S_{o,n}$  may then be calculated based on given values for  $S_{i,n}$  and  $C$ . The input slew and total capacitance values may be estimated using a timing model of the receiving gate. However, in many cases, especially for modern processes, wires have non-negligible resistance. Therefore, using the total capacitance as the load  $C$  of a gate when calculating the gate delay and the output slew may introduce inaccuracy. In such cases, an effective capacitance may be used in equations (4) and (5) instead of the total capacitance. The effective capacitance,  $C_{eff}$ , of the load may be determined with an iterative method, and used to more precisely approximate the actual load in terms of output delay [Pileggi]. The iterative method may be performed using an interconnect simplification, and may involve expansive numerical computations. Therefore, if the nets have a large resistance, one can use the iterative method of determining  $C_{eff}$ , and store the parameters of the simplified net for later use.

[0032] In general, using  $C_{tot}$  as the receiver load in Eq.(2) can provide the correct ordering of output timing events according to their corresponding arrival times. For example, the delay is usually a monotonic function of output load, and  $C_{eff}$  is usually close to the total (lumped) capacitance  $C_{tot}$  of the driven net. Therefore,  $C_{tot}$  instead of  $C_{eff}$  may usually be used in equations (4) and (5) to select the worst-case timing event. This avoids a need in expensive processing of the output net and  $C_{eff}$  iterations.

[0033] The values  $C_{tot}$  and  $S_i$  for a given gate, which are used to calculate the output delays and output slews, may be available from a library of timing models, such as LIBERTY [lib\_ref] or TLF[tlf\_ref]. For example, the library may store a delay model of a gate, including the input slew and capacitive load data of the gate, in a table of a library, as shown in Table 1.

$C_{tot}$	10fF	30fF	100fF	300fF
$S_i$				
20ps	30ps	40ps	80ps	200ps
50ps	50ps	70ps	100ps	250ps
200ps	80ps	120ps	180ps	350ps
500ps	150ps	200ps	260ps	450ps

**Table 1: Delay table for gate as a function of input slew and output load**

The columns of **Table 1** are headed by capacitive load data, and the rows are headed by input  
 5 slew data. The data for the capacitive load and input slew values shown in **Table 1** may be  
 determined from the results of a number of circuit simulations. For example, the slew of the  
 input transition may be determined by the difference between simulated crossing times of  
 selected threshold voltages,  $V_{th1}$  and  $V_{th2}$ , of the transition. Also, when using the tabular format,  
 an appropriate interpolation between available values may be performed during the analysis.

10 **[0034]** The delay and slew data may be also fitted using cubic splines having  
 coefficients that are also stored in tables in a library. For example, the coefficients stored in  
**Tables 2** and **3** are used in TLF expressions to determine gate delay and output slew values.

Tables 2 and 3: Examples of spline representation of data in TLF format

Cell(ssad2
...
TIMING_Model(ioDelayRise Model0
timing_by_trans_and_cap0Mod
(spline
data
(
(0.202000 0.273000 0.517000 1.496000)
(0.272000 0.344000 0.641000 1.566000)
(0.325000 0.396000 0.691000 1.614000)
(0.415000 0.489000 0.794000 1.717000)
)
)
)
)
Table 3
TLF Load Table
TIMING_Model(SlopeRiseModel0
timing_by_trans_and_cap_0Mod
(Spline
data
(
(0.173000 0.316000 0.983000 3.090000)
(0.179000 0.324000 0.986000 3.090000)
(0.189000 0.333000 0.991000 3.092000)
(0.219000 0.366000 1.020000 3.106000)
)
)
)
)

[0035] After determining the gate delay and output slew by introducing the input slew and load capacitance values to equations (4) and (5), the arrival times of the transitions at the receiver output are then founded as:

$$T_{o,n} = T_{i,n} + D_n \quad (6)$$

[0036] The worst-case timing event selected for the further propagation in the max delay analysis is that having latest arrival time:

$$\max\{T_{o,n}\}, \text{ for } n=1 \dots N \quad (7)$$

[0037] For the min delay analysis one needs to choose a minimum of arrival times instead of maximum.

[0038] To illustrate the receiver dependent selection process, and to quantify the improvement over conventional methods, consider an example of the stage shown in **Figure 3**.

The driver is an inverter from a 0.13u-technology industrial library skewed towards the low voltage, meaning that n-device is stronger than the p-device. Results of simulations of the circuit for two different transitions at the input are shown in **Figure 4**. The two input transitions are linear saturated ramps of 20 ps and 120 ps, respectively, and arrival times differ by 30 ps (as  
5 defined by using  $V_{ref}$  equal to 50% of  $V_{dd}$ ).

[0039] The two transitions on the output node N of the skewed inverter have close slews, but as is shown in **Figure 4**, the input transition with the worse input slew, which is the linear ramp marked with rectangular boxes, has the output transition with the earlier arrival time, which is the transition curve marked with circles. The transition with the later input arrival time,  
10 which is the ramp marked with diagonal crosses, has a better input slew and a later output arrival time, as shown by the curve marked with horizontal and vertical crosses. If a conventional selection criterion is used, then the input with the sharper input slew (the ramp with the diagonal crosses) is chosen as the worst-case transition, and leads to a ~20% underestimation of delay on this stage. If the worse input slew is combined with worse output arrival time to form a new  
15 timing event to be propagated further, then a 25% overestimation (conservative) on this stage would occur. The receiver dependent worst-case selection method described is therefore more efficient in selecting the worst-case transition from a plurality of transitions with different arrival times and slews, which in this example is the ramp with the better input slew (the ramp with diagonal crosses).

20 [0040] Practical examples of situations where the receiver dependent method improves the simulation results include converging paths, unbalanced stacks, critical path fixing and optimization, and noise-on-delay effects.

[0041] **Converging paths.** Timing events with different arrival times and slews can emerge due to converging paths. For example, most gates of circuit designs have more than one  
25 input. If two or more inputs of a gate receive transitions with very different slews, it is probable that the output transitions will also have different slews. This may cause an inversion of the arrival times of the transitions on subsequent stages, especially if the stages are skewed.

[0042] **Unbalanced stacks.** Unbalanced strength of device stacks in complex gates can also lead to significant differences in slews of the output transitions. An example of such a  
30 circuit is shown in **Figure 5**. The circuit has two gates, a driver-complex gate  $NOT(A0 * A1 + B)$ ,

and a receiver-inverter. The complex gate  $\text{NOT}(A0 \cdot A1 + B)$  has different strengths of pull-down stacks corresponding to vectors with switching inputs  $B$  and  $A1$ , respectively. The different strengths of the two vectors cause the two rising transitions  $B$  and  $A1$  at the node  $N$  to have different output slews at the node  $OUT$ , and as a result, the earlier/later arrival times of the transitions are inverted at the receiver's output.

[0043] For example, the simulation results of two transitions on inputs  $A0$  and  $B$  of the circuit of **Figure 5** are shown in **Figure 6**, by the two saturated ramps. The input transition to  $A0$  is shown in the ramp marked with diamond boxes, and the input transition to  $B$  is shown by the ramp having a solid line. The output transitions at the output of the driver have different slews and arrival times: transition  $B$  has the faster input slew, but has an output transition that arrives later than the output corresponding to input transition  $A0$ , as shown by the output transition for the input to  $B$ , which is marked with circles, as compared with the output transition for the input to  $A0$ , which is marked with crosses. As a result, the responses on the output of inverter arrive in an order that is the opposite of the order of their input slews. For example, the transitions at the output node  $OUT$ , show that the transition caused by the input to node  $B$  (the curve marked with rectangular boxes) arrives later than the transition caused by the input to node  $A0$  (the curve marked with diagonal boxes). Therefore, the input signal which arrives earlier on nodes  $A1$  and  $N$  has the worst-case transition, and is selected to be propagated on the inverter output,  $OUT$ .

[0044] **Critical path fixing and circuit optimization.** During a fixing stage of the design chain, gates belonging to a critical path are often upsized. This affects (mostly improves) both the arrival time and slew of a timing event on the input of the next gate. Although the arrival time is the target of the stage optimization, the improved slew may, depending on the skew property of the receiving gate, have a significant impact on the arrival time on the next stage. The receiver-dependent selection method is therefore more accurate than tools using the conventional worst-case event selection method, because they usually neglect this slew improvement, which may lead to usage of a sub-optimal cell.

[0045] For example, **Figure 7** shows simulation results for two inverters of different sizes, each having the circuit design of **Figure 3**. The simulation results are obtained by applying the same input transition to the different drivers, which is represented by the linear

saturated ramp of 50ps, which is marked with rectangular boxes. The original inverter has sizes  $p/n = 1.92u/1.12u$ . The upsized driver is a stronger inverter having sizes  $p/n = 3.84u/2.52u$ . The output of the smaller driver to node N is shown by the curve marked with crosses. The output transition of the signal from the smaller driver to node OUT is shown by the curve marked with diamonds. The output of the bigger driver on node N is shown by the curve marked with circles, and the output transition at node OUT is shown by the curve marked with triangles.

[0046] As seen in **Figure 7**, the delay on the receiver's input improves by ~11ps when the driver's size is increased. Conventional analysis criterion leads to an over-design of the circuit, because the improved slew on the output of the inverter reduces the delay. The receiver dependent selection process leads to a more efficient design, because the effects of the improved slew rate can be considered based on measurements at the output of receiver. The simulation result of upsizing on the delay that is determined with the receiver dependent selection method therefore becomes significantly more accurate, at ~17ps.

[0047] **Noise-on-delay effect.** Several tools provide the ability to account for coupling noise effects on delay [CTE/celtic]. The noise effects, such as the logic correlation between victim and aggressor nets, can lead to different slews and arrival times for the transitions at the input and output of the victim net. An example of such a circuit shown in **Figure 8**. The aggressor net *B* causes a push-out and increase of slew of the transition on the victim net *N* when both are transitioning in opposite directions, such as when the falling transition on *N* is caused by rising transition on *B*. However, the net *B* should not be included in the list of active (switching) aggressors when the falling transition on *N* is caused by rising transition on *A*, since this would violate the sensitization. Therefore, in the case of significant coupling between *N* and *B*, the difference in slews may be accounted for using the receiver dependent method.

[0048] The receiver-dependent static timing analysis provides a method, which indicates how to choose a signal to be propagated to the next gate in the design. The method includes determining an output slews and arrival times for each signal that is input to a gate, based on a timing model of the gate, and selecting a worst delay input signal from the input signals based on the output slews or delays, or both. For example, the signal with the worst output delay as a function of input slew may be selected. Also, the signal with the worst output slew as a function of input slew may be selected. The timing model of the receiving gate is used

to find which of the timing events will cause the worst-case arrival time of a signal at a sampling element on the path. The disclosed method therefore provides more accurate and conservative selection criteria for identifying the worst-case timing. It also improves quality of circuit optimization for example helping to minimize over-design of driver upsizing.

5           **[0049]** The timing analysis method may be performed by an automated process, where a computer readable medium stores a computer program that has instructions for performing receiver-dependent static timing analysis. A computer or processor that receives the computer instructions from the computer memory device then executes the instructions to perform the analysis. In the automated process, the circuit design to be analyzed may include a virtual circuit  
10 block with enough information to calculate the output timing delays. The circuit design may, for example, be in a netlist format, with the gates referred to in the netlist being pre-characterized to the extent necessary to perform the timing analysis. Information about timing (i.e., propagation) delays across the gates in the netlist may be stored in a timing library format (TLF) expression or in any other suitable format.

15           **[0050]** These and other embodiments of the present invention may be realized in accordance with the above teachings and it should be evident that various modifications and changes may be made to the above described embodiments without departing from the broader spirit and scope of the invention. The specification and drawings are, accordingly, to be regarded in an illustrative rather than restrictive sense and the invention measured only in terms  
20 of the claims.